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Mechanics of Fluid - II (AM 404)

Time: 3 Hrs.

Full Marks: 70

Use separate answer scripts for each half  
Answer six questions taking three from each half  
All questions are of equal value  
Two marks are reserved for neatness in each half

FIRST HALF

Derive the expressions for stresses  $\sigma_r$  and  $\sigma_{\theta}$  in cylindrical coordinate system.

Derive the equation of the principle of the conservation of linear momentum for an incompressible laminar flow in the r-direction in cylindrical co-ordinate system. State and apply all the assumptions required.

- a) Derive the expression of Mach numbers across a normal shock.
- b) What is the relation between stagnation density across a normal shock?
- c) Derive the expression for Rayleigh Pilot tube formula.

Consider a Mach 3 flow. It is desired to slow the flow to a subsonic speed. Consider two separate ways for achieving this: (1) the Mach 3 flow is slowed by passing directly through a normal shock wave; (2) the Mach flow first deflected through an oblique shock with a 40° wave angle, and then subsequently through a normal shock. Calculate the ratio of final total pressure values for the

It is required to determine the displacement thickness, momentum thickness and coefficient of drag in terms of streamwise coordinate and Reynolds number for a two dimensional, incompressible and laminar flow over a flat plate held parallel to the flow.

Second Half

- 6A) Flow takes place from a larger diameter pipe to a smaller diameter pipe, which is coaxially fitted sufficiently inside the larger pipe. Assuming the pressure in the annular space between the two pipes is equal to the total pressure in the larger diameter pipe deduce an expression for loss of head due to friction in terms of cross-sectional area of two pipes and velocity in smaller pipe.
- b) A horizontal pipe, 100 mm in diameter, is joined by sudden enlargement to a 150 mm diameter pipe. Water is flowing through it at the rate of 2 m<sup>3</sup>/min. Find the loss of head due to abrupt expansion and the pressure difference in the two pipes. If the change of section is gradual without any loss, what would be the change in pressure?
- 7.a) A pipe of length 'X' and diameter 'd' is fitted with a nozzle at its exit. A constant head 'H\*' is maintained at the inlet to the pipe. Determine the nozzle tip diameter so that the power transmitted through the pipe-nozzle assembly is a maximum.
- b) Calculate the power required to pump sulphuric acid (viscosity 0.04 Ns/m<sup>2</sup> and specific gravity 1.83) at 45 lit/sec from a supply tank to a storage tank. The two tanks are connected by a glass-lined pipe of 150 mm diameter and 15 m length. The liquid level in the storage tank is 6 m above that in supply tank. Assume for turbulent flow in the pipe,  $f = 0.0056(1 + 100 N^{-1/4})$  and for laminar flow  $f = 64/N$ . Neglect minor losses.
- g) An oil flows from an open vessel at the rate of 1.7 cc/sec through a 450 mm long and 2.5 mm bore vertical tube. The oil surface in the vessel is 600 mm above the lower end of the tube. Neglecting the exit velocity and assuming fully developed laminar flow throughout the entire tube, determine the dynamic viscosity of the oil.
- b) Two reservoirs, A and C, are connected through a 300 mm diameter pipeline 1 km long. At a point B in the pipeline, 300 mm from reservoir A, a valve is fitted on a short branch pipe, laid in parallel to the main pipe, which discharges into atmosphere. The valve may be considered as an orifice with  $C_d = 0.65$ . If the friction factor  $f$  for all pipes is 0.03, calculate the rate of discharge to the reservoir C when the valve on the branch line at B is fully open. Also estimate the flow through the short pipe into atmosphere.
- 9. A main pipe consists of a quadrilateral network of pipes ABCD and a triangular network of pipes ADE, the pipe AD being common to both networks. The resistances of the pipes AB, BC, CD, DA, AE and DE are 4, 2, 5, 4, 2 and 3 units respectively. A flow of 10 units enters the entire network at E and flows of 3, 4 and 3 units leave the network at B, C and D respectively. Estimate, by Hardy-Cross method, the flow rates in each pipe upto an accuracy of 0.1 units of flow and indicate their directions on a sketch.

10. Write short notes on any three of the following:

- (a) Water Hammer ; (b) Economic Pipe Diameter (c) Uniform Sub Layer (d) Mach Cone (e) Stokes law for flow around a sphere.