

Time: 3 hours

Full Marks: 70

Answer any Six questions taking Three from each half

Each question carries equal marks

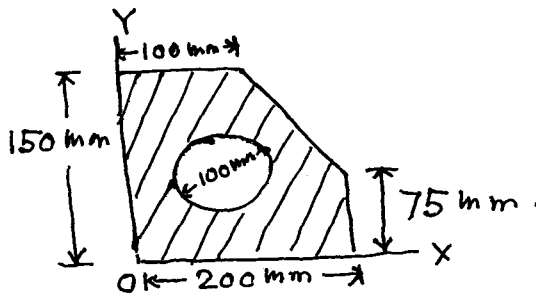
2 marks kept reserved for neatness in each half

Assume suitable data, if required

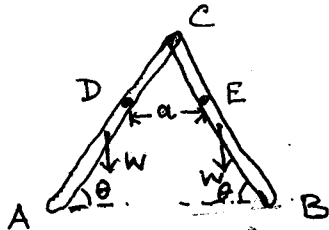
Notations used have their conventional meaning

FIRST HALF

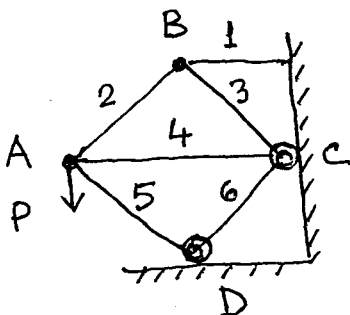
- Q.1. Determine the co-ordinates x_c and y_c of the center of a 100 mm diameter circular hole cut in a thin plate so that this point will be the centroid of the remaining shaded area.



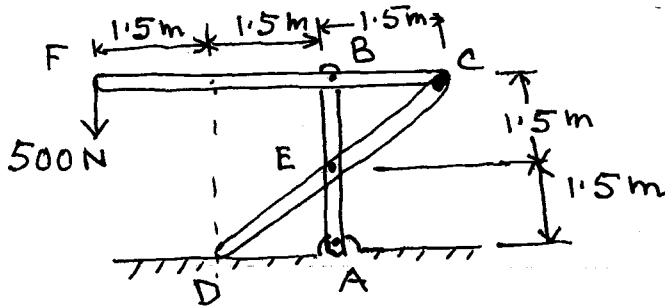
- Q.2. Two slender prismatic bars AC and BC, each of length, l and weight W are hinged together at C and supported in a vertical plane by two pegs at D and E. Neglecting all friction, find the angle, θ that each bar will make with the horizontal in the condition of equilibrium.



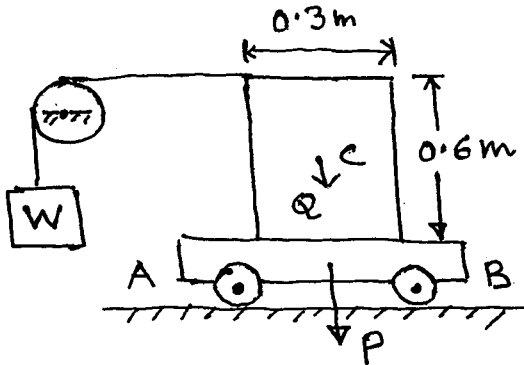
- Q.3. Determine the magnitude and nature of axial force in each bar of the plane truss supported and loaded as shown in figure. ABCD is a square and AC is horizontal. Show result in tabular form.



- Q.4. Calculate the shear forces on the pins A, B, C and E of the plane frame supported and loaded as shown in the figure. Neglect weight of the members and assume smooth horizontal floor. At A there is hinge support.



- Q.5. A rectangular block of weight, $Q = 890 \text{ N}$ rests on a flat car of weight, $P = 445 \text{ N}$ which may roll along the horizontal plane AB without friction. The car and block together are to be accelerated by the weight W arranged as shown in the figure. Assuming that there is sufficient friction between the block and the car to prevent sliding, find the maximum value of the weight W by which the car can be accelerated. What will this acceleration be?



SECOND HALF

- Q.6. Two smooth circular cylinders (refer to Fig. Q6), each of weight, $W = 445 \text{ N}$ and radius, $r = 152 \text{ mm}$ are connected at their centers by a string AB of length, $l = 406 \text{ mm}$ and rest upon a horizontal plane, supporting above them a third cylinder of weight, $Q = 890 \text{ N}$ and radius, $r = 152 \text{ mm}$. Find the force, S in the string and the reactions at the points of contact D and E.
- Q.7. A smooth right circular cylinder of radius, r rests on a horizontal plane and is kept from rolling by an inclined string AC of length, $2r$. A prismatic bar AB of length, $3r$ and weight, Q is hinged at point A and leans against the roller. Find the tension, S in the string AC. (refer to Fig. Q7)
- Q.8. Two blocks having weights W_1 and W_2 are connected by a string and rest on horizontal planes. If the angle of friction for each block is ϕ , find the magnitude and direction of the least force, P applied to the upper block that will induce sliding. (refer to Fig. Q8)
- Q.9. Two heavy right circular rollers of diameters D and d respectively rest on a rough horizontal plane. The larger roller has a string wound around it to which a horizontal force P can be applied. Assuming that the coefficient of friction μ has the same value for all surfaces of contact, determine the necessary condition under which the large roller can be pulled over the small one. (refer to Fig. Q9)
- Q.10. Determine the coordinates x_c and y_c of the centroid C of the area between the parabola $y = \frac{x^2}{a}$ and the straight line $y = x$. (refer to Fig. Q10)

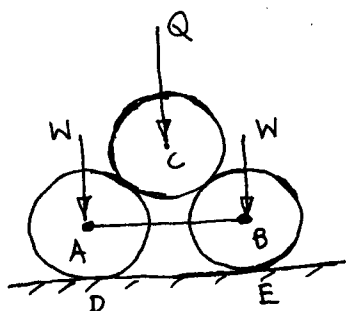


Fig. Q6

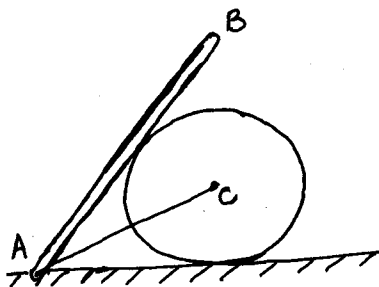


Fig. Q7

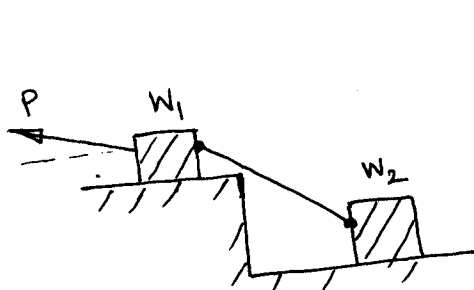


Fig. Q8

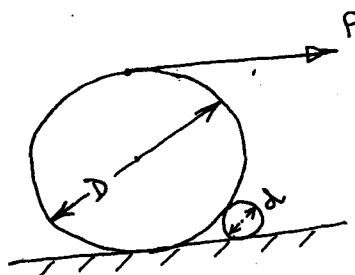


Fig. Q9

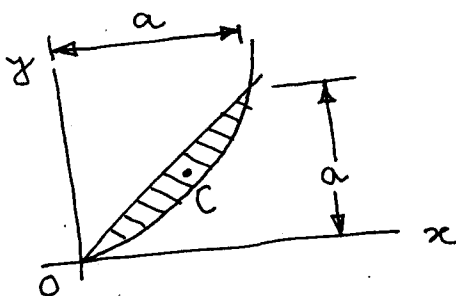


Fig. Q10