

**M.E. (Civil) 1<sup>st</sup> Semester Examination, 2011**

**SUBJECTT: STABILITY OF STRUCTURES (CE-903)**

Full marks –100

Time: 3 Hours

The questions are of equal value.  
Answer any five questions.

1. Obtain the critical load  $P_{cr}$  for a column of length  $L$  and uniform flexural rigidity  $EI$ . The column has bottom end fixed and top end hinged.
2. A both ends hinged column with varying moment of inertia has stiffness given by  $EI$  for the portion  $0.3L$  on the both end and  $3EI$  for the central portion  $0.4L$ . Calculate the critical load using Newmark's method and estimate the percentage of maximum error.
3. Calculate the buckling load of a flagpole having uniform rigidity  $EI$ , length  $L$  and self weight  $q$  per unit length.
4. (a) Using energy method obtain the expression for Rayleigh's Quotient and also its modified form for the assessment of critical load for buckling of a column.  
(b) Obtain the critical load for a pin-end strut on elastic foundation of modulus of foundation,  $\beta$ . The strut has uniform moment of inertia  $I$  and length  $L$ .
5. (a) Derive the differential equation for a both end hinged column considering the effect of shearing force on the critical load.  
(b) Calculate the critical load of a built-up column having both end hinged. The column has cross diagonal lacing bars.
6. Derive the differential equation of equilibrium of a plate subjected to combined bending and tension.
7. A rectangular plate simply supported along two opposite side perpendicular to the direction of uniformly compressed load. Obtain the critical load.

8. Using finite difference techniques obtain the buckling load for a column having one bottom end fixed and top end hinged. The column has uniform moment of rigidity  $EI$  and span  $L$ . Also obtain the mode shape.
9. A prismatic simply supported beam  $AB$  of flexural rigidity  $EI$  and span  $L$  is hinged at  $A$ . The beam is subjected to moment at  $A$  and axial force at  $B$ . Derive the expression for slopes at  $A$  &  $B$ .
10. A single bay portal with beam of span length  $5\text{m}$ , height of column  $10\text{m}$  has both ends hinged. The beam is subjected to an uniformly distributed load  $50\text{ t/m}$  in addition to a concentrated load of  $45\text{ t}$  acting as axial force in each column. Assume constant rigidity  $EI\ 10,000\text{ t-m}^2$ . Draw the bending moment diagram considering the effect of axial force. Given  $\psi(u)$  for  $u = 1.3, 1.35, 1.4$  are  $1.1345, 1.1473, 1.1610$  respectively.