

Time: 3 hours

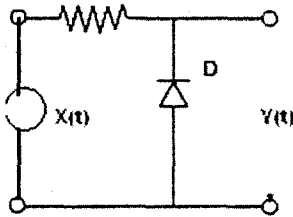
Full marks: 70

Answer any FIVE questions

1. a) The probability density function(PDF) of a Gaussian signal  $X(t)$  is given by

$$p_X(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-x^2/2\sigma^2}$$

The signal is applied to the input of a half-wave rectifier circuit (Fig.1). Assuming an ideal diode, determine probability density function (PDF) and cumulative distribution function (CDF) of the output signal amplitude  $Y$ .



**Fig.1**

- b) Let  $X(t)$  be a stationary process with mean  $\mu_X$  and autocorrelation function  $R_X(\tau)$ . This process is applied to an LTI system with impulse response  $h(t)$ . Determine the mean and autocorrelation function of the output process as a function of  $h(t)$ ,  $\mu_X$  and  $R_X(\tau)$ .
2. a) Write an analytical expression of an 8-PSK modulated signal and draw its constellation diagram.  
b) Derive an expression of the bit error rate in BFSK modulation scheme considering the presence of additive white Gaussian Noise.
3. a) A pair of signals  $s_i(t)$  and  $s_k(t)$  have a common duration  $T$ . Show that

$$\int_0^T (s_i(t) - s_k(t))^2 dt = \| \underline{s}_i - \underline{s}_k \|^2$$

Where  $\underline{s}_i$  and  $\underline{s}_k$  denote the vector representations of the signals  $s_i(t)$  and  $s_k(t)$  respectively

- b) Establish the equivalence between a correlation receiver and a matched filter for detection of binary signals in additive White Gaussian noise.

4. With a neat block diagram explain the operation of a MSK modem. Write down its key advantages over BPSK, QPSK and BFSK. Compare the performance of MSK modulation with that of GMSK.  
7+3+4
5. Explain the concept of spread spectrum modulation. Derive an expression for the power of a narrowband jamming signal at the output of spread DSSS/BPSK receiver. Hence justify the following: the processing gain of a spread spectrum system may be expressed as the ratio of the spread bandwidth of the transmitted signal to the bandwidth of message signal for a DSSS/BPSK system. Make necessary assumptions.  
3+7+4
6. Write down some applications of spread spectrum modulation. Explain the advantages of multicarrier modulation over single carrier modulation. With a neat block diagram, discuss the principle of operation an OFDM communication.  
3+4+7
7. Write down short notes on any **two**
- Gaussian Process
  - Maximum likelihood decoding
  - Frequency hopping spread spectrum modulation