

M.E. (Civil) 2nd Semester Final Examination, April, 2013
Plastic Analysis of Structures
(CE – 1001)

Full Marks – 70

Time Allowed – 3 Hours

Answer any Five questions.

1. Explain plastic hinge, shape factor and different types of mechanisms of plastic collapse. Determine the shape factor for a steel I-section made of 180 mm x 32 mm thick top flange plate, 450 mm x 12 mm thick web plate and 120 mm x 32 mm thick bottom flange plate.
2. State and explain Static and Kinematic theorems used in plastic analysis. A beam of length L and fully plastic moment capacity M_p is simply supported at one end and fixed at the other end. The beam is subjected to a concentrated load W at a distance of $2L/3$ from the fixed end. Find the collapse value of load W and show the positions of plastic hinges indicating their chronological development.
3. A continuous beam ABC is simply supported at the three supports A, B and C. $AB = 6.0$ m and $BC = 10.0$ m with a central concentrated load of $2W$ on span AB and an uniformly distributed load of $W/5$ on the entire span of BC. The beam has a uniform section with fully plastic moment $M_p = 400$ kNm. Determine the loads at the formation of the first and second plastic hinges in the continuous beam ABC.
4. In a rectangular portal frame ABCD the support A and the support D are fixed. The columns AB and CD are vertical with heights 4.0m and 5.0m respectively. The beam BC is horizontal with a span of 10.0m. The fully plastic moment capacities of AB, BC and CD are M_p , $3M_p$ and $1.5M_p$ respectively. A vertical load of $2P$ acts at mid span of BC and a horizontal load P acts at B towards C. Find the collapse load P and draw the Bending Moment Diagram at collapse.
5. An inclined portal frame PQRS has P and S fixed. Column PQ is vertical with height 4.0m. Beam QR is horizontal with span 7.0m and RS is 5.0m long with an inclination of 60° with vertical. A vertical load $2W$ acts on QR at 4.0m distance from Q and a horizontal load W acts at Q towards R. Determine the collapse load and draw the bending moment diagram at collapse. Assume fully plastic moment capacity M_p all through.
6. Coordinates of the joints of a fixed base doubly inclined portal frame are given in metres as (0, 0), (3, 6), (13, 6) and (16, 1) respectively. A vertical load of P acts on the top beam at 4m distance from the left end of the beam and a horizontal load of $P/2$ acts from left to right at the top beam level. Find the collapse load and draw the collapse bending moment diagram. Assume M_p as constant.
7. A two span portal with left span $1.25L$ and right span $0.75L$ has equal column heights L and bottom ends fixed. Left column and left beam are with $2.0M_p$ where other beam and columns are with $1.5M_p$. Two vertical loads of P each act at mid-point of beams and a horizontal load $P/2$ acts from left to right at the beam level. Find the collapse load and draw the plastic bending moment diagram to check whether it is a true collapse load or not.
8. Find the minimum weight of a portal with span $1.5L$ and height L having bottom ends fixed and M_p value for the beam and two columns as M_a and M_b respectively. The portal is subjected to a vertical load P at the centre of the beam and another load P from left to right at the beam level.